

Course Title: Signals and Systems  
Date: May 30<sup>th</sup>, 2013

Course Code: CCE2210  
Allowed time: 3 Hours

Year: 2<sup>nd</sup> Comp.  
No. of Pages:

**Remarks:** You must show all of your work -- partial credit may be given to partially correct answers, while answers with no justification may not receive full points. Please attempt all questions.

**Problem (1) (35 Marks)**

a) For the block diagram given in Fig.1

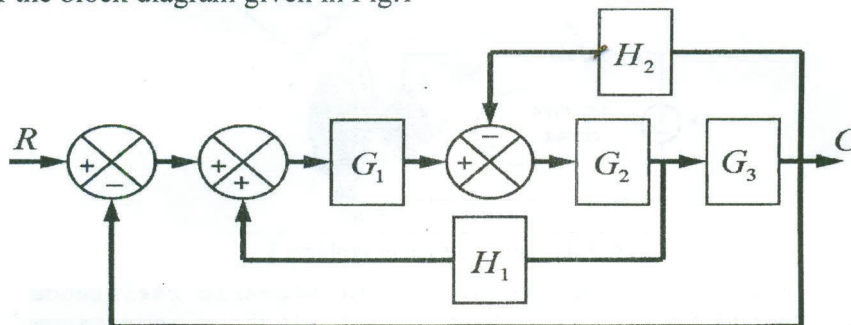


Fig. 1: Block diagram of problem 1-a

- i- Using block diagram reduction rules, find the system transfer function (10 Marks)
- ii- Check your answer using signal flow graph technique (10 Marks)

b) The state-space representation of a satellite system is given by:

$$\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} x(t) + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u(t)$$

$$y(t) = \begin{bmatrix} 0 & 1 \end{bmatrix} x(t)$$

- i- Find the system transfer function (5 Marks)
- ii- Calculate the state-transition matrix  $\Phi(t)$  (4 Marks)
- iii- Check the system controllability and observability (6 Marks)

**Problem (2) (25 Marks)**

a) Discuss the stability of the closed loop system shown in Fig. 2 in terms of K and determine the value of K which results in critical stability. (10 Marks)

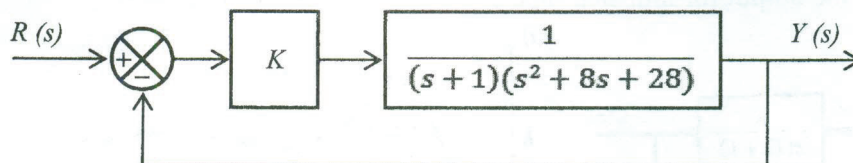


Fig. 2: Block diagram of problem 2-a

b) Consider the system shown in Fig. 3.

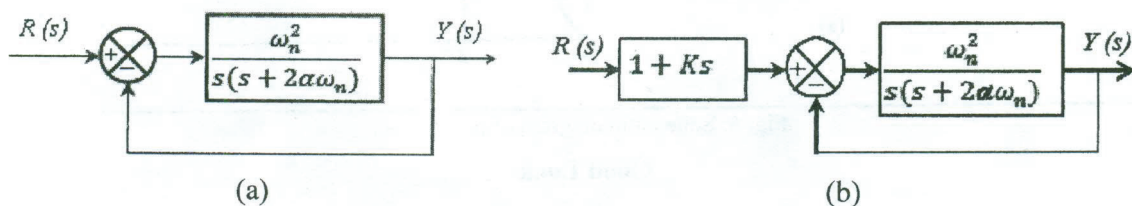


Fig. 3: Block diagram of problem 2-b

- i- For Fig.3-a, show that the steady-state error  $e_{ss}$  for unit ramp input is equal to  $2\alpha/\omega_n$   
 ii- Show that  $e_{ss}$  is eliminated if the input is introduced to the system through proportional plus derivative element as shown in Fig. 3-b and the value of  $K$  is properly set. (10 Marks)

**Problem (3) (20 Marks)**

The electric equivalent circuit of the armature and the free-body diagram of the rotor of a DC motor are shown in Fig.4. The definitions of the physical parameters are:

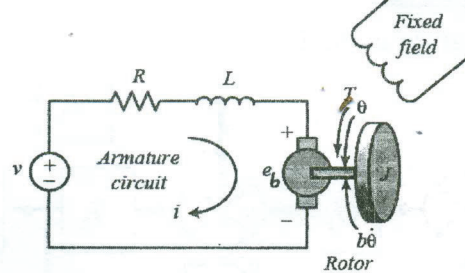


Fig. 4: Schematic diagram of problem 3

- |  |   |
|--|---|
| (J) moment of inertia of the rotor             | (R) electric resistance                 |
| (b) motor viscous friction constant            | (L) electric inductance                 |
| (K <sub>b</sub> ) electromotive force constant | (K <sub>t</sub> ) motor torque constant |

- i- Write the system equations and show that its block diagram representation is as in Fig. 5  
 ii- Drive a state-space representation using current, angular velocity, and angular position as the states of the system (10 Marks)

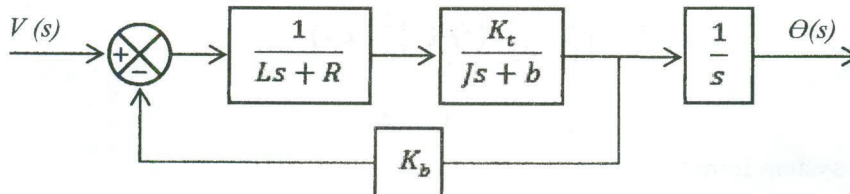


Fig. 5: Schematic diagram of problem 3-i

**Problem (4) (10 Marks)**

When the system shown in Fig. 6-a is subjected to a unit step input, the system output responds as shown in Fig. 6-b. Determine the values of  $K$  and  $T$  using the response curve and then find an expression for the output for unit step input.

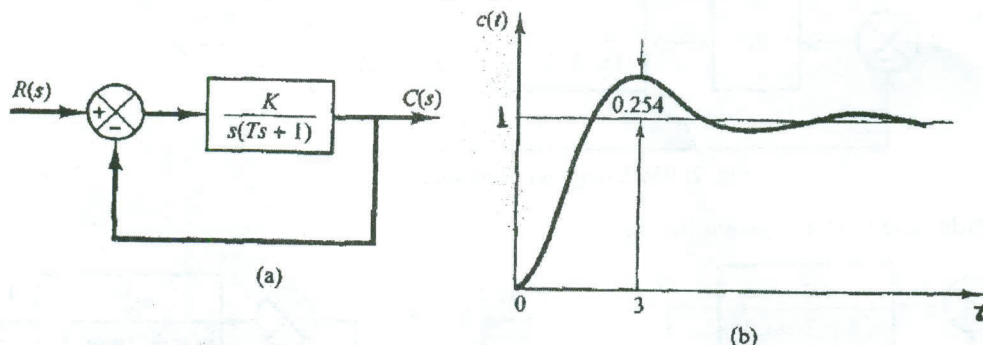


Fig. 6: Schematic diagram of problem 4

Good Luck